

The following sequence is defined recursively. Use iteration to guess an explicit formula for the sequence.

$$e_k = 4e_{k-1} + 5, \text{ for all integers } k \geq 1.$$

$$e_0 = 2$$

After that, use mathematical induction to verify the correctness of the formula you obtained.