

1. Find two functions f and g so that the given function is the composition of f and g .

a) $y = (x^3 - 7x)^5$ b) $y = \sin^4(3x - 8)$ c) $y = (2 + \sin(x))^5$

2. Find the derivatives of the following functions.

a) $f(x) = -2x^2 + 6$ b) $f(x) = \frac{5 \cos(3x)}{x^2 + 2}$ c) $f(x) = e^{x^2}$

3. Let $f(x) = (x - 1)(x - 3) = x^2 - 4x + 3$.

Use the definition of the derivative to find $f'(2)$

4. Determine $D(e^{3x} \cdot \sin(5x + 7))$ and $d/dx(\cos(x \cdot e^x))$.

5. Given that $D(\arcsin(x)) = \frac{1}{\sqrt{1-x^2}}$, compute the derivatives $D(\arcsin(5x))$ and $\frac{d}{dx}(\arcsin(x^2))$

6. For each function in problems a-c, write y as a function of u for some u

that is a function of x .

a. $y = (x^3 - 7x)^5$ b. $y = \sin^4(3x - 8)$ c. $y = (2 + \sin(x))^5$

7. If two functions are equal, then their derivatives are also equal. In a,b differentiate each side of the trigonometric identity to get a new identity.

a. $\sin^2(x) = 1/2 - 1/2 \cos(2x)$ b. $\cos(2x) = \cos^2(x) - \sin^2(x)$

8. For problems a-c, calculate $y' = \frac{dy}{dx}$:

a. $y = Ax^3 - B$ b. $y = e^{Ax} + e^{-Ax}$ c. $y = \cos(Ax + B)$

9. In problems a- c, calculate $f'(x) \cdot x'(t)$ when $t = 3$ and use these values to determine the value of $\frac{d}{dt}(f(x(t)))$ when $t = 3$.

a. $f(x) = \cos(x)$, $x = t^2 - t + 5$ b. $f(x) = e^x$, $x = \sin(t)$ c. $f(x) = \sqrt{x}$, $x = 2 + \frac{21}{t}$

10. Determine whether the following statements are true or false.

a. $\lim_{x \rightarrow 2} (x^2 + x - 2) = 10$

b. $f(x)$ is continuous at 1.

$$f(x) = \begin{cases} 1 - x & x < 1 \\ x^2 - 2x + 1 & x \geq 1 \end{cases}$$

c. $f(x)$ is differentiable at -1

$$f(x) = \begin{cases} -2x & x < -1 \\ x^2 & x \geq -1 \end{cases}$$